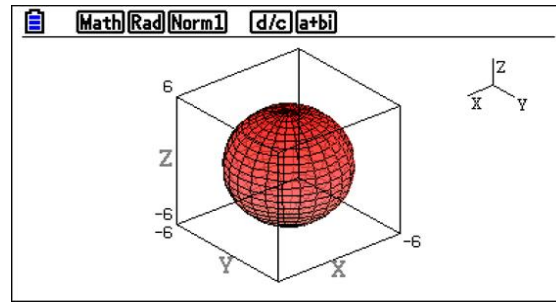


MONDAY



TUESDAY



WEDNESDAY

THURSDAY

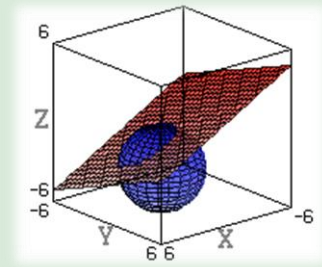


FRIDAY

SATURDAY

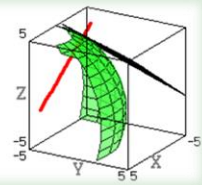
SUN.

1 Let the sphere be the equation:
 $E \equiv x^2 + y^2 + z^2 - 2x + 6z = 0$.
 Determine the coordinates of the centre and the radius measure. Check if the plan:
 $\Pi \equiv 3x - 2y + 6z + 1 = 0$
 and the sphere are secant. Determine the radius of the intersecting circle of E, Π .
 Determine the centre of the intersection circle of E, Π .

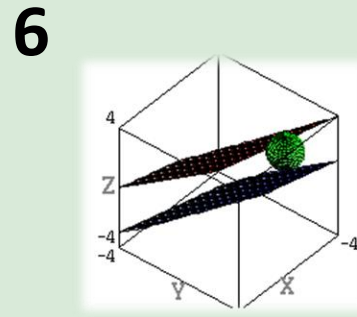
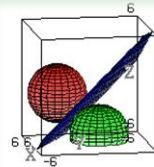


3

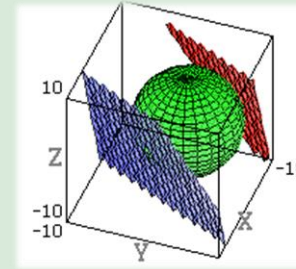
4 Find the equation of the sphere with centre C (3, -5, -2) tangent to the plane:
 $2x - y - 3z + 11 = 0$



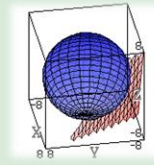
5 Find the equation of the sphere of radius 3, which is tangent to the plane $x + 2y + 2z + 3 = 0$ at the point A (1, 1, -3)



7 Determine the equation of the sphere that is tangent to the planes:
 $\Pi \equiv 6x - 3y - 2z - 35 = 0$
 $\Omega \equiv 6x - 3y - 2z + 63 = 0$
 knowing that the point M (5, -1, -1) is a point of tangency in one of the planes.

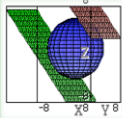


9 Determine the equation of the plane tangent to the sphere
 $x^2 + y^2 + z^2 = 49$
 at point M (6, -3, -2)

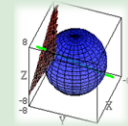


10

11 Determine the equations of the planes tangent to the sphere
 $(x - 3)^2 + (y + 2)^2 + (z - 1)^2 = 25$
 parallel to plane $4x + 3z - 17 = 0$

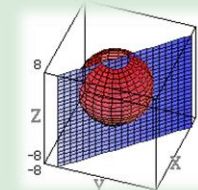


Show that the plane $2x - 6y + 3z - 49 = 0$ is tangent to the sphere
 $x^2 + y^2 + z^2 = 49$
 Calculate the coordinates of the point of tangency

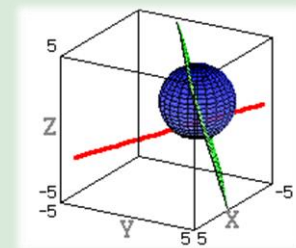


13 A sphere has its centre on the line
 $r \equiv \begin{cases} 2x + 4y - z - 7 = 0 \\ 4x + 5y + z - 14 = 0 \end{cases}$
 and is tangent to the planes
 $\Pi \equiv x + 2y - 2z - 2 = 0$
 $\Omega \equiv x + 2y - 2z + 4 = 0$
 Determine its equation.

14 Determine the equation of the circumference that passes through the points A (3, -1, -2), B (1, 1, -2) and C (-1, 3, 0)

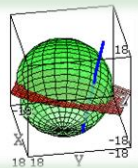


15 Determine the relative position of the line
 $r \equiv \begin{cases} x = 2 - 2\alpha \\ y = -\frac{7}{2} + 3\alpha \\ z = -2 + \alpha \end{cases}$
 and the sphere
 $E \equiv x^2 + y^2 + z^2 + x - 4y - 3z + \frac{1}{2} = 0$

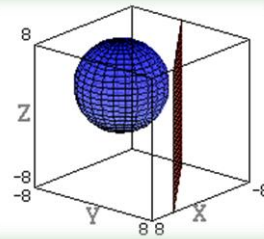


17

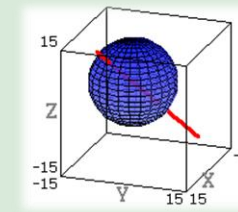
18 Determine the equation of the sphere with centre O (2, 3, -1) that intersects the line
 $s \equiv \begin{cases} 5x - 4y + 3z + 20 = 0 \\ 3x - 4y + z - 8 = 0 \end{cases}$
 with a chord of length equal to 16.



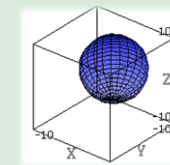
19 In the sphere of equation
 $(x - 1)^2 + (y + 2)^2 + (x - 3)^2 = 25$
 determines the point M closest to the plane
 $\Pi \equiv 3x - 4y + 19 = 0$
 and calculate the distance from point M to this plane.



21 Find the shortest distance from point A (1, -1, 3) to the sphere
 $E \equiv x^2 + y^2 + z^2 - 6x + 4y - 10z - 62 = 0$
 At what point on the sphere is the shortest distance achieved?

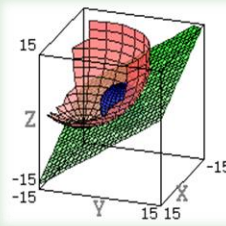


23 Determine the equation of the sphere that passes through the points A (3, 1, -3); B (-2, 4, 1); C (-5, 0, 0) and has the center in the plane:
 $\Pi \equiv 2x + y - z + 3 = 0$

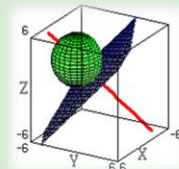


24

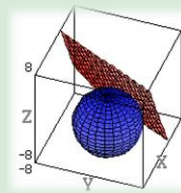
25 Let the spheres be equations:
 $E_1 \equiv x^2 + y^2 + z^2 = 25$
 $E_2 \equiv x^2 + y^2 + z^2 - 10x + 15y - 25z = 0$
 Prove that the two spheres are secant. Determine the plane that contains the intersection of the two spheres. Determine the centre and radius of the intersecting circle.



27 Prove that the point T (1, 0, 1) belongs to the plane:
 $\pi \equiv x - 2y + 2z = 3$
 Determine the equation of the sphere that passes through the point P (1, 0, 5) and is tangent at T to the π plane.



28 Determine the equation of the plane tangent to the sphere:
 $(x - 3)^2 + (y - 1)^2 + (z + 2)^2 = 24$
 passing through point M (-1, 3, 0)



29 Let the sphere:
 $x^2 + y^2 + z^2 - 6x - 4y + 8z + 20 = 0$
 Find the sphere of equal radius, exterior tangent at point A (1, 4, -3) of the sphere. Find the sphere of equal radius, exterior tangent at the point diametrically opposite to point A on the sphere.

